

Source parameter relationship of asperity model

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In order to understand the difference between the asperity model and crack model, we have investigated the source parameter relationship of asperity model. Asperities are distributed on the fault area, the rest of the fault area being the background area, where non-zero stress drop are considered. Slip on asperities is proportional to asperity radius and stress drop, and the coefficient is larger than in the case of crack model. Slip on the background area is described as proportional to the average asperity stress drop. By using the reciprocal theorem to the crack model and asperity model, and by putting the total moment of asperity model equal to that of crack model, we have got the relationship between the slip coefficient for asperities and the background. We have set the trial function for the asperity slip coefficient as,

$$g_a \cdot e_a = (e_a^2 + n \cdot e_b^2)^{1/3},$$

where g_a is the asperity slip coefficient in concern, e_a^2 the total asperity area over fault area, e_b^2 the background area over fault area, and n the ratio of background stress drop to average asperity stress drop.

When $e_a^2=0.3$ and $n=0.1$, asperity slip is 30% larger than the crack slip, while $e_a^2=0.2$ and $n=0.1$, it is 40% larger. When $e_a^2=0.3$ and $n=0.1$, or when $e_a^2=0.2$ and $n=0.2$, the asperity slip is twice as large as the average slip of entire fault, which is found for large earthquakes.

As the asperity slip is derived to be larger than the crack slip, the slip velocity on asperity is almost the same with the slip velocity of the crack with the same stress drop. Thus the slip duration time of asperity is shown to be longer than the slip duration of crack with the same stress drop and the radius. The corner frequency of seismic radiation is determined by the slip duration and the source size. The long duration of slip in case of asperity model results in smaller corner frequency than in the case of crack model.

Hence we can uniquely specify all the necessary parameters for strong motion prediction based on the slip coefficient of asperity model.

アスベリティモデルにおける震源パラメタの関係
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(A) クラックモデル

- S : 断層全体の面積($S=\pi r^2$)
 M_0 : 地震モーメント
 C_b : 変位の係数
 $M_0=\mu S D_b$ (1)
 $D_b=C_b(\Delta\sigma/\mu) r$ (2)

(B) アスベリティ

- S_{am} : m 番目のアスベリティの面積($S_{am}=\pi r_{am}^2$)
 D_{am} : アスベリティでの平均変位
 M_{0am} : アスベリティでの地震モーメント
 $\Delta\sigma_{am}$: アスベリティでの応力降下量
 g_{am} : アスベリティ変位の係数
 $\varepsilon_{am}^2=S_{am}/S$ (3)
 $\varepsilon_a^2=\sum \varepsilon_{am}^2$ (4)
 $\Delta\sigma_a=\sum \Delta\sigma_{am} \varepsilon_{am}^2/\varepsilon_a^2$ (5)
 $D_{am}=g_{am} C_b(\Delta\sigma_{am}/\mu) r_{am}$
 $=g_{am} \varepsilon_{am} C_b(\Delta\sigma_{am}/\mu) r$ (6)
 $M_{0am}=\mu S D_{am} \varepsilon_{am}^2$
 $=\pi g_{am} \varepsilon_{am}^3 C_b \Delta\sigma_{am} r^2$ (7)
 $g_{am} \geq 1$ (8)
 $g_a=\sum (g_{am} \varepsilon_{am}^3 \Delta\sigma_{am}) / (\varepsilon_a^3 \Delta\sigma_a)$ (9)

(C) 背景領域

- S_b : 背景領域の面積($S_b=\pi r_b^2$)
 $\Delta\sigma_b$: 背景領域での応力降下量
 D_b : 背景領域での平均変位

- M_{0b} : 背景領域での地震モーメント
 g_b : 背景領域変位の係数
 $a_b^2=S_b/S$ (10)
 $\nu=\Delta\sigma_b/\Delta\sigma_b \leq 1$ (11)
 $D_b=g_b C_b(\Delta\sigma_b/\mu) r_b$
 $=g_b a_b C_b(\Delta\sigma_b/\mu) r$ (12)
 $M_{0b}=\mu S D_b a_b^2$
 $=\pi g_b a_b^3 C_b \Delta\sigma_b r^2$ (13)
 $g_b \geq 0$ (14)

(D) 相互関係

- $M_0=\sum M_{0am}+M_{0b}$ (15)
 $\Delta\sigma_a=\sum g_{am} \varepsilon_{am}^3 \Delta\sigma_{am}+g_b a_b^3 \Delta\sigma_b$ (16)
 $\Delta\sigma_a=\sum \varepsilon_{am}^2 \Delta\sigma_{am}+a_b^2 \Delta\sigma_b$
 $=\Delta\sigma_a(\varepsilon_a^2+\nu a_b^2)$ (17)
 $\sum g_{am} \varepsilon_{am}^3 \Delta\sigma_{am}+g_b a_b^3 \Delta\sigma_b$
 $=(\varepsilon_a^2+\nu a_b^2) \Delta\sigma_a$ (18)
 $g_b=(\varepsilon_a^2+\nu a_b^2-g_a \varepsilon_a^3)/a_b^3$ (19)

(E) $\nu \rightarrow 1$ のとき

- $g_{am} \rightarrow 1/\varepsilon_{am}$ (20)
 $g_b \rightarrow 1/a_b$ (21)

(F) $\nu < 0$, $D_b \rightarrow 0$

- $g_{am} \rightarrow 1$ (22)
 $g_b \rightarrow 0$ (23)
 $\nu \geq (\varepsilon_a^3 - \varepsilon_a^2)/a_b^2$ (24)

(G) $g_{am}=(\varepsilon_a^2+\nu a_b^2)^{1/3}/\varepsilon_{am}$ (25)

- $g_b=(\varepsilon_a^2+\nu a_b^2)^{1/3}/a_b$ (26)